

Chapter Three

Theory of Consumer Behaviour

Consumer behaviour can be best understood in three steps.

First, by examining consumer's preference, we need a practical way to describe how people prefer one good to another.

Second, we must take into account that consumers face budget constraints – they have limited incomes that restrict the quantities of goods they can buy.

Third, we will put consumer preference and budget constraint together to determine consumer choice.

Consumer preferences

- In order to tell whether one bundle is preferred to another, we see how the consumer behaves in choice situations involving two bundles.
- If she always chooses X when Y is available, then it is natural to say that this consumer prefers X to Y .
- We use the symbol $\succ$ to mean that one bundle is strictly preferred to another, so that $X \succ Y$ should be interpreted as saying that the consumer strictly prefers X to Y , in the sense that she definitely wants the X -bundle rather than the Y -bundle.
- If the consumer is indifferent between two bundles of goods, we use the symbol $\sim$ and write $X \sim Y$.
- Indifference means that the consumer would be just as satisfied, according to her own preferences, consuming the bundle X as she would be consuming bundle Y .
- If the consumer prefers or is indifferent between the two bundles we say that she weakly prefers X to Y and write $X \succeq Y$.

The concept of utility

- Economists use the term *utility* to describe the *satisfaction or pleasure derived from the consumption of a good or service*.
- In other words, utility is the power of the product to satisfy human wants. Given any two consumption bundles X and Y, the consumer definitely wants the X-bundle than the Y-bundle if and only if the utility of X is better than the utility of Y.

- *In defining utility, it is important to bear in mind the following points.*
- *‘Utility’ and ‘Usefulness’ are not synonymous. For example, paintings by Picasso may be useless functionally but offer great utility to art lovers. Hence, usefulness is product centric whereas utility is consumer centric.*
- *Utility is subjective. The utility of a product will vary from person to person.*
- *That means, the utility that two individuals derive from consuming the same level of a product may not be the same.*
- *For example, non-smokers do not derive any utility from cigarettes.*
- *Utility can be different at different places and time. For example, the utility that we get from drinking coffee early in the morning may be different from the utility we get during lunch time.*

Approaches of measuring utility

- There are two major approaches to measure or compare consumer's utility: cardinal and ordinal approaches.
- The cardinalist school postulated that utility can be measured objectively.
- According to the ordinalist school, utility is not measurable in cardinal numbers rather the consumer can rank or order the utility he derives from different goods and services.

The cardinal utility theory

- According to the cardinal utility theory, utility is measurable by arbitrary unit of measurement
- called **utils in the form of 1, 2, 3 etc.** For **example, we may say that consumption of an orange** gives Bilen 10 utils and a banana gives her 8 utils, and so on.
- From this, we can assert that Bilen gets more satisfaction from orange than from banana.

Assumptions of cardinal utility theory

The cardinal approach is based on the following major assumptions.

- 1. Rationality of consumers. The main objective of the consumer is to maximize his/her satisfaction given his/her limited budget or income.** Thus, in order to maximize his/her satisfaction, the consumer has to be rational.
- 2. Utility is cardinally measurable. According to the cardinal approach, the utility or satisfaction of each commodity is measurable.** Utility is measured in subjective units called utils.
- 3. Constant marginal utility of money. A given unit of money deserves the same value at any time or place it is to be spent.** A person at the start of the month where he has received monthly salary gives equal value to 1 birr with what he may give it after three weeks or so.
- 4. Diminishing marginal utility (DMU). The utility derived from each successive units of a commodity diminishes.** In other words, the marginal utility of a commodity diminishes as the consumer acquires larger quantities of it.
- 5. The total utility of a basket of goods depends on the quantities of the individual commodities. If there are n commodities in the bundle with quantities $X_1, X_2, \dots, X_n$, the total utility is given by $TU = f(X_1, X_2, \dots, X_n)$.**

Total and marginal utility

- **Total Utility (TU)** is the total satisfaction a consumer gets from consuming some specific quantities of a commodity at a particular time.
- As the consumer consumes more of a good per time period, his/her total utility increases.
- However, there is a saturation point for that commodity beyond which the consumer will not be capable of enjoying any greater satisfaction from it.
- **Marginal Utility (MU)** is the *extra satisfaction a consumer realizes from an additional unit of* the product. In other words, marginal utility is the change in total utility that results from the consumption of one more unit of a product.
- Graphically, it is the slope of total utility. Mathematically, marginal utility is:

Mathematically, marginal utility is:

$$MU = \frac{\Delta TU}{\Delta Q}$$

where, ΔTU is the change in total utility, and ΔQ is the change in the amount of product consumed.

To explain the relationship between TU and MU, let us consider the following hypothetical example.

Continued....

Table 3.1: Total and marginal utility

Quantity	Total utility (TU)	Marginal utility (MU)
0	0	-
1	10	10
2	18	8
3	24	6
4	28	4
5	30	2
6	30	0
7	28	-2

Graphically, the above data can be depicted as follows.

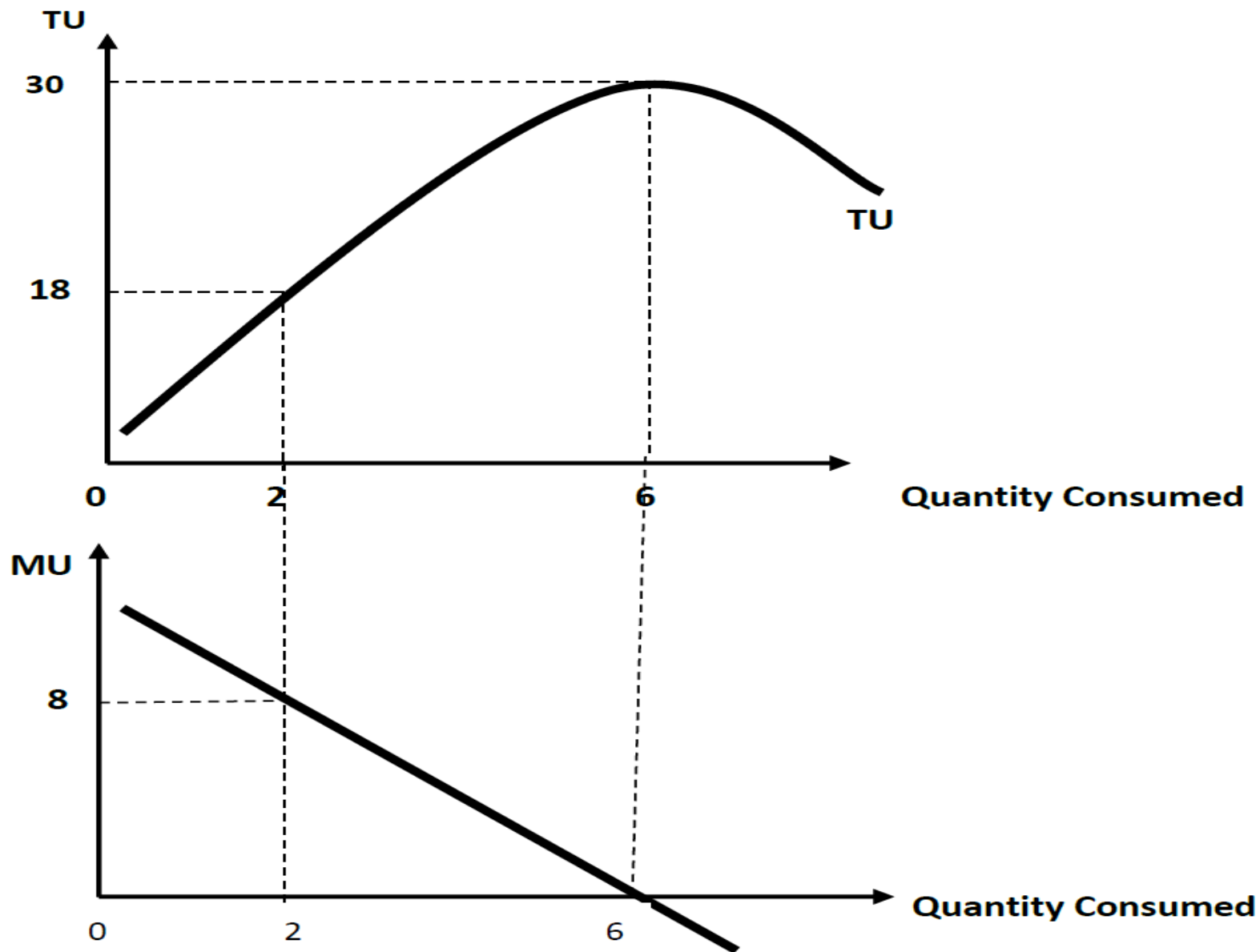


Figure 3.1: Total and marginal utility curves

As it can be observed from the above figure,

- When TU is increasing, MU is positive.
- When TU is maximized, MU is zero.
- When TU is decreasing, MU is negative.

Law of diminishing marginal utility (LDMU)

The *law of diminishing marginal utility* states that as the quantity consumed of a commodity increases per unit of time, the utility derived from each successive unit decreases, consumption of all other commodities remaining constant.

In other words, the extra satisfaction that a consumer derives declines as he/she consumes more and more of the product in a given period of time.

- The law of diminishing marginal utility is based on the following assumptions.
- The consumer is rational
- The consumer consumes identical or homogenous product.
- The commodity to be consumed should have similar quality, color, design, etc.
- There is no time gap in consumption of the good
- The consumer taste/preferences remain unchanged

Equilibrium of a consumer

- The objective of a rational consumer is to maximize total utility.
- As long as the additional unit consumed brings a positive marginal utility, the consumer wants to consume more of the product because total utility increases.

a) the case of one commodity

The equilibrium condition of a consumer that consumes a single good X occurs when the marginal utility of X is equal to its market price.

$$MU_X = P_X$$

Proof

Given the utility function

$$U = f(X)$$

If the consumer buys commodity X, then his expenditure will be $Q_X P_X$. The consumer maximizes the difference between his utility and expenditure.

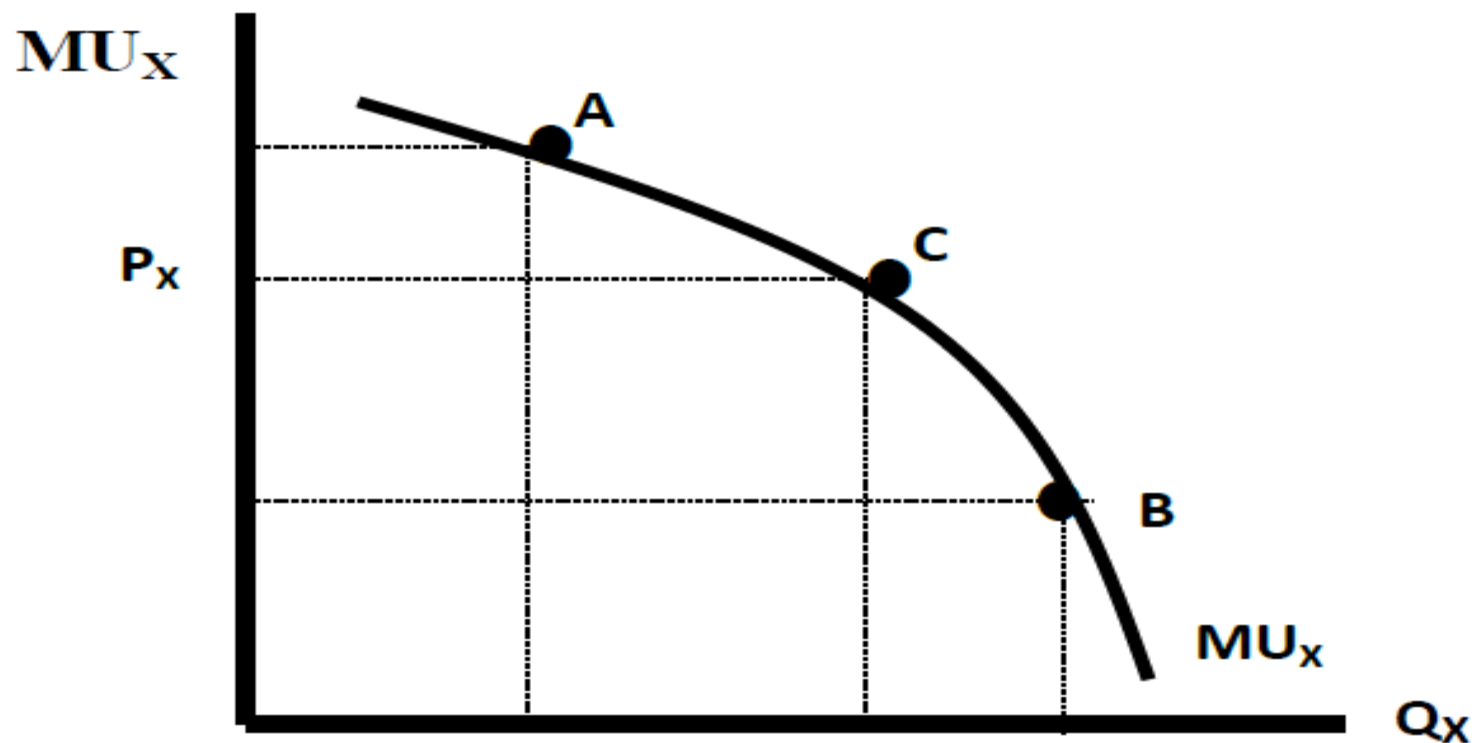
$$\text{Max}(U - Q_X P_X)$$

The necessary condition for maximization is equating the derivative of a function to zero.

Thus,

$$\frac{dU}{dQ_X} - \frac{d(Q_X P_X)}{dQ_X} = 0$$

$$\frac{dU}{dQ_X} - P_X = 0 \Rightarrow MU_X = P_X$$



Equilibrium condition of consumer with only one commodity

At any point above point C (like point A) where $MU_X > P_X$, it pays the consumer to consume more. When $MU_X < P_X$ (like point B), the consumer should consume less of X. At point C where $MU_X = P_X$ the consumer is at equilibrium.

b) the case of two or more commodities

For the case of two or more goods, the consumer's equilibrium is achieved when the marginal utility per money spent is equal for each good purchased and his money income available for the purchase of the goods is exhausted. That is,

$$\frac{MU_X}{P_X} = \frac{MU_Y}{P_Y} = \dots = \frac{MU_N}{P_N} \quad \text{and} \quad P_X Q_X + P_Y Q_Y + \dots + P_N Q_N = M$$

where, M is the income of the consumer.

Example: Suppose Saron has 7 Birr to be spent on two goods: banana and bread. The unit price of banana is 1 Birr and the unit price of a loaf of bread is 4 Birr. The total utility she obtains from consumption of each good is given below.

Utility schedule for two commodities

Income = 7 Birr, Price of banana = 1 Birr, Price of bread = 4 Birr

<i>Banana</i>				<i>Bread</i>			
<i>Quantity</i>	<i>TU</i>	<i>MU</i>	<i>MU/P</i>	<i>Quantity</i>	<i>TU</i>	<i>MU</i>	<i>MU/P</i>
0	0	-	-	0	0	-	-
1	6	6	6	1	12	12	3
2	11	5	5	2	20	8	2
3	14	3	3	3	26	6	1.5
4	16	2	2	4	29	3	0.75
5	16	0	0	5	31	2	0.5
6	14	-2	-2	6	32	1	0.25

Recall that utility is maximized when the condition of marginal utility of one commodity divided by its market price is equal to the marginal utility of the other commodity divided by its market price.

$$\text{i) } MU_1/P_1 = MU_2/P_2$$

$$\frac{MU_{banana}}{P_{banana}} = \frac{MU_{bread}}{P_{bread}} = \frac{3}{1} = \frac{12}{4} = 3$$

$$\text{ii) } P_1.Q_1 + P_2.Q_2 = M$$

$$(1*3) + (4*1) = 7$$

The total utility that Saron derives from this combination can be given by:

$$TU = TU_1 + TU_2$$

$$TU = 14 + 12$$

$$TU = 26$$

Given her fixed income and the price level of the two goods, no combination of the two goods will give her higher TU than this level of utility.

Limitation of the cardinal approach

1. The assumption of cardinal utility is doubtful because utility may not be quantified. Utility cannot be measured absolutely (objectively).
2. The assumption of constant MU of money is unrealistic because as income increases, the marginal utility of money changes.

The ordinal utility theory

- **In the ordinal utility approach**, it is not possible for consumers to express the utility of various commodities they consume in absolute terms, like 1 util, 2 utils, or 3 utils but it is possible to express the utility in relative terms.
- The consumers can rank commodities in the order of their preferences as 1st, 2nd, 3rd and so on.
- Therefore, the consumer need not know in specific units the utility of various commodities to make his choice.

Assumptions of ordinal utility theory

- The ordinal approach is based on the following assumptions.
- **Consumers are rational** - they maximize their satisfaction or utility given their income and market prices.
- **Utility is ordinal** - *utility is not absolutely (cardinally) measurable. Consumers are required only to order or rank their preference for various bundles of commodities.*
- **Diminishing marginal rate of substitution**: The marginal rate of substitution is the rate at which a consumer is willing to substitute one commodity for another commodity so that his total satisfaction remains the same.
- The rate at which one good can be substituted for another in consumer's basket of goods diminishes as the consumer consumes more and more of the good.

- The **total utility of a consumer** is measured by the amount (quantities) of all items
- he/she consumes from his/her **consumption basket**.
- **Consumer's preferences are consistent.** For example, if there are three goods in a given
- consumer's basket, say, X, Y, Z and if he prefers X to Y and Y to Z, then the consumer is expected to prefer X to Z.
- This property is known as axioms of **transitivity**. The ordinal utility approach is explained with the help of indifference curves.
- Therefore, the ordinal utility theory is also known as the *indifference curve approach*.

Indifference set, curve and map

- ***Indifference set/ schedule*** is a combination of goods for which the consumer is indifferent.
- It shows the various combinations of goods from which the consumer derives the same level of satisfaction.

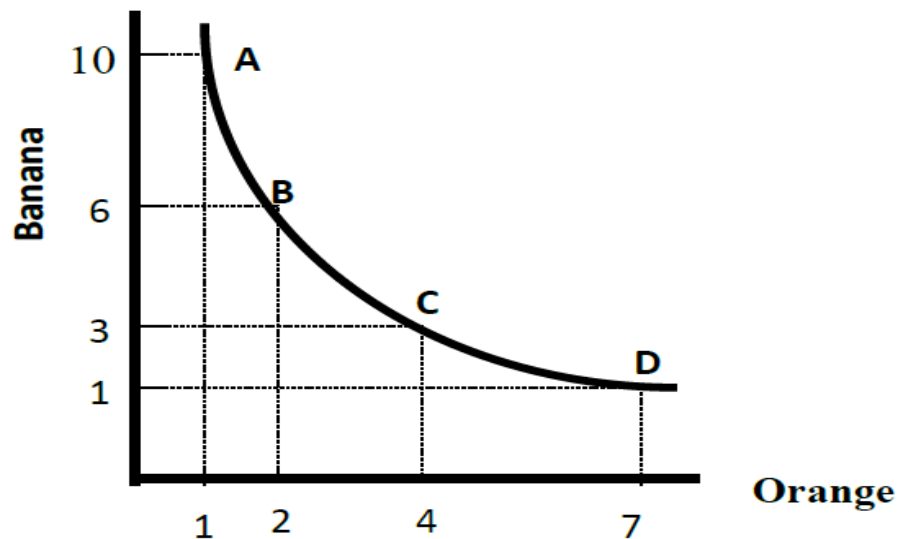
Consider a consumer who consumes two goods X and Y (table 3.3).

Table 3.3: Indifference schedule

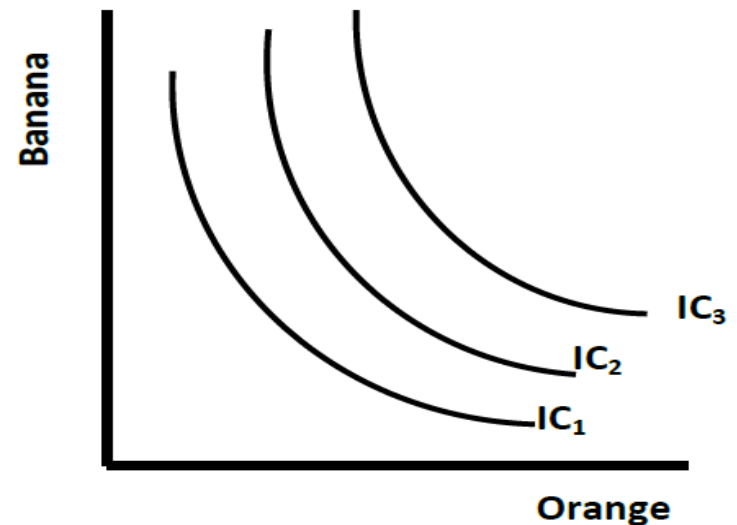
Bundle (Combination)	A	B	C	D
Orange	1	2	4	7
Banana	10	6	3	1

In table 3.3 above, each combination of good X and Y gives the consumer equal level of total utility. Thus, the individual is indifferent whether he consumes combination A, B, C or D.

Indifference curve: When the indifference set/schedule is expressed graphically, it is called an *indifference curve*. An indifference curve shows different combinations of two goods which yield the same utility (level of satisfaction) to the consumer. A set of indifference curves is called **indifference map**.



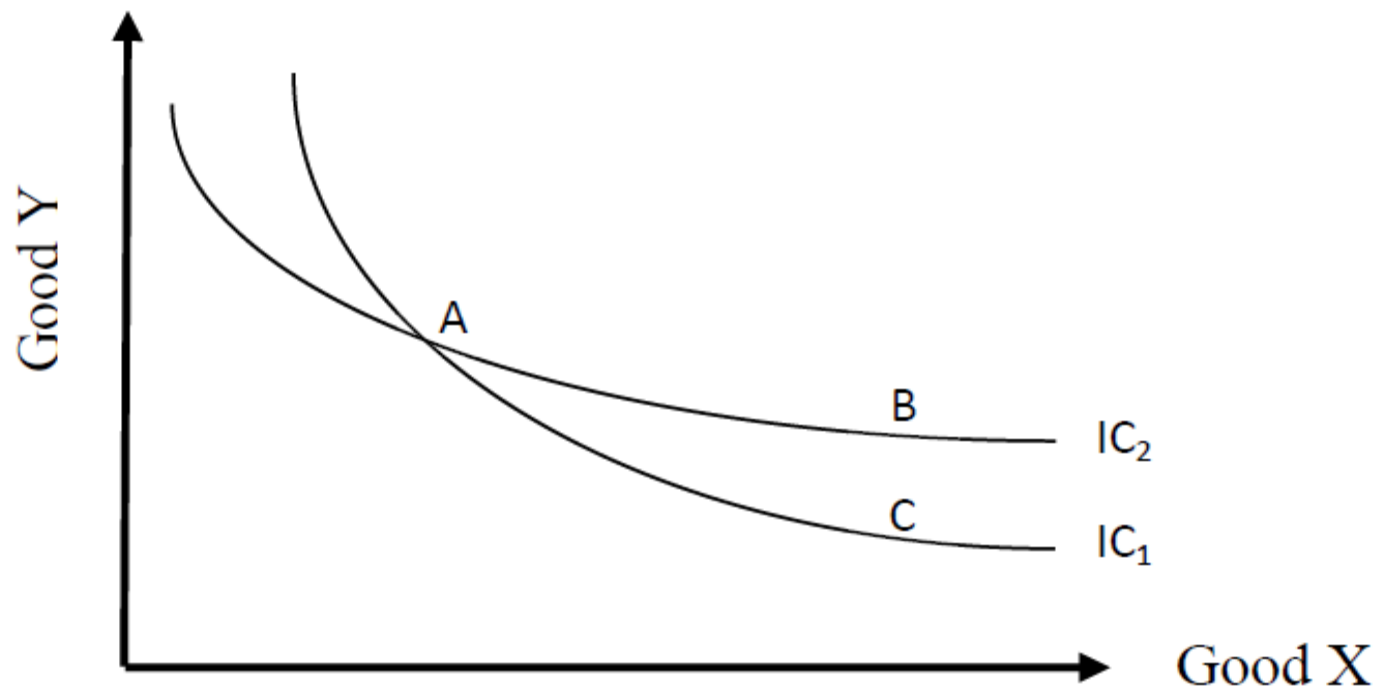
i) Indifference curve



ii) Indifference map

Properties of indifference curves

- 1. Indifference curves have negative slope (downward sloping to the right).** Indifference curves are negatively sloped because the consumption level of one commodity can be increased only by reducing the consumption level of the other commodity.
- 2. Indifference curves are convex to the origin.** This implies that the slope of an indifference curve decreases (in absolute terms) as we move along the curve from the left downwards to the right.
 - The convexity of indifference curves is the reflection of the diminishing marginal rate of substitution.
- 3. A higher indifference curve is always preferred to a lower one.** *The further away from the origin an indifferent curve lies, the higher the level of utility it denotes.*
 - Baskets of goods on a higher indifference curve are preferred by the rational consumer because they contain more of the two commodities than the lower ones.
- 4. Indifference curves never cross each other (cannot intersect).** The assumptions of consistency and transitivity will rule out the intersection of indifference curves. Figure 3.4 shows the violations of the assumptions of preferences due to the intersection of indifference curves.



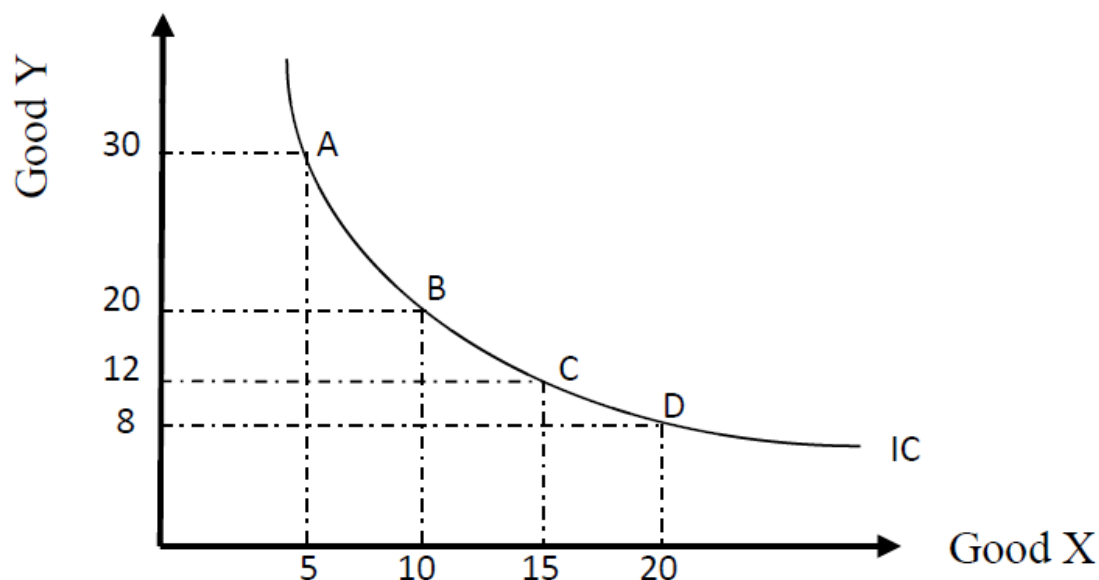
In the above figure, the consumer prefers bundle B to bundle C. On the other hand, following indifference curve 1 (IC_1), the consumer is indifferent between bundle A and C, and along indifference curve 2 (IC_2) the consumer is indifferent between bundle A and B. According to the principle of transitivity, this implies that the consumer is indifferent between bundle B and C which is contradictory or inconsistent with the initial statement where the consumer prefers bundle B to C. Therefore, indifference curves never cross each other.

Marginal rate of substitution (MRS)

Marginal rate of substitution of X for Y is defined as the number of units of commodity Y that must be given up in exchange for an extra unit of commodity X so that the consumer maintains the same level of satisfaction. Since one of the goods is sacrificed to obtain more of the other good, the MRS is negative. Hence, usually we take the absolute value of the slope.

$$MRS_{X,Y} = \frac{\text{Number of units of } Y \text{ given up}}{\text{Number of units of } X \text{ gained}} = -\frac{\Delta Y}{\Delta X}$$

To understand the concept, consider the following indifference curve.



It is also possible to derive MRS using the concept of marginal utility. $MRS_{X,Y}$ is related to MU_X and MU_Y as follows.

$$MRS_{X,Y} = \frac{MU_X}{MU_Y}$$

Proof: Suppose the utility function for two commodities X and Y is defined as:

$$U = f(X, Y)$$

Since utility is constant along an indifference curve, the total differential of the utility function will be zero.

$$dU = \frac{\partial U}{\partial X} dX + \frac{\partial U}{\partial Y} dY = 0$$

$$MU_X dX + MU_Y dY = 0$$

$$\frac{MU_X}{MU_Y} = -\frac{dY}{dX} = MRS_{X,Y} \quad \text{Similarly, } \frac{MU_Y}{MU_X} = -\frac{dX}{dY} = MRS_{Y,X}$$

Example: Suppose a consumer's utility function is given by $U(X, Y) = X^4 Y^2$. Find $MRS_{X,Y}$

Solution: $MRS_{X,Y} = \frac{MU_X}{MU_Y}$

$$MU_X = \frac{\partial U}{\partial X} = 4X^3 Y^2 \quad \text{and} \quad MU_Y = \frac{\partial U}{\partial Y} = 2X^4 Y \quad \text{Hence, } MRS_{X,Y} = \frac{MU_X}{MU_Y} = \frac{4X^3 Y^2}{2X^4 Y} = \frac{2Y}{X}$$

The budget line or the price line

Do you think that the indifference curve discussed in the previous section tells us whether a given combination of goods is affordable to the consumer? If no, what are the major constraints to the consumer in maximizing his/her total utility?

Indifference curves only tell us about consumer preferences for any two goods but they cannot show which combinations of the two goods will be bought. In reality, the consumer is constrained by his/her income and prices of the two commodities. This constraint is often presented with the help of the budget line.

The *budget line* is a set of the commodity bundles that can be purchased if the entire income is spent. It is a graph which shows the various combinations of two goods that a consumer can purchase given his/her limited income and the prices of the two goods.

In order to draw a budget line facing a consumer, we consider the following assumptions.

- There are only two goods bought in quantities, say, X and Y.
- Each consumer is confronted with market determined prices, P_X and P_Y .
- The consumer has a known and fixed money income (M).

Assuming that the consumer spends all his/her income on the two goods (X and Y), we can express the budget constraint as:

$$M = P_X X + P_Y Y$$

By rearranging the above equation, we can derive the following general equation of a budget line.

$$Y = \frac{M}{P_Y} - \frac{P_X}{P_Y} X$$

Graphically,

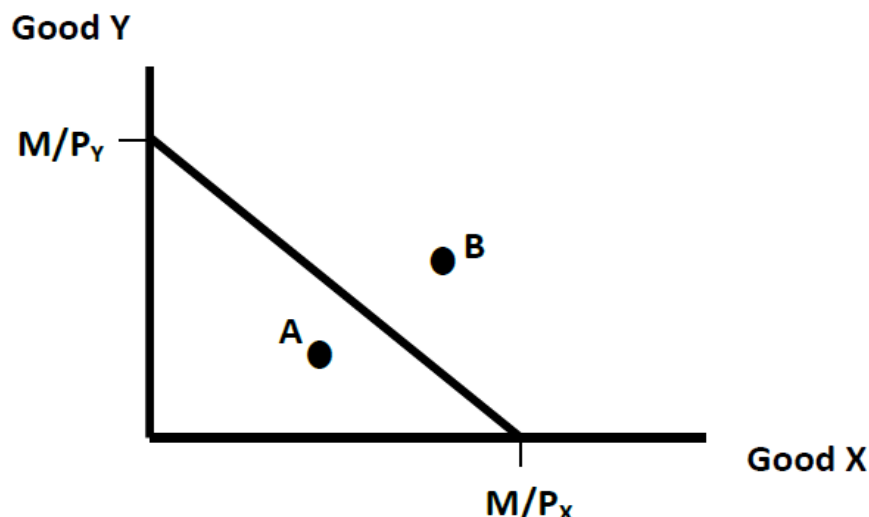


Figure 3.6: The budget line

Note that:

- The slope of the budget line is given by $-\frac{P_X}{P_Y}$ (the ratio of the prices of the two goods).
- Any combination of the two goods within the budget line (such as point A) or along the budget line is attainable.
- Any combination of the two goods outside the budget line (such as point B) is unattainable (unaffordable).

Example: A consumer has \$100 to spend on two goods X and Y with prices \$3 and respectively. Derive the equation of the budget line and sketch the graph.

Solution: The equation of the budget line can be derived as follows.

$$P_X X + P_Y Y = M$$

$$3X + 5Y = 100$$

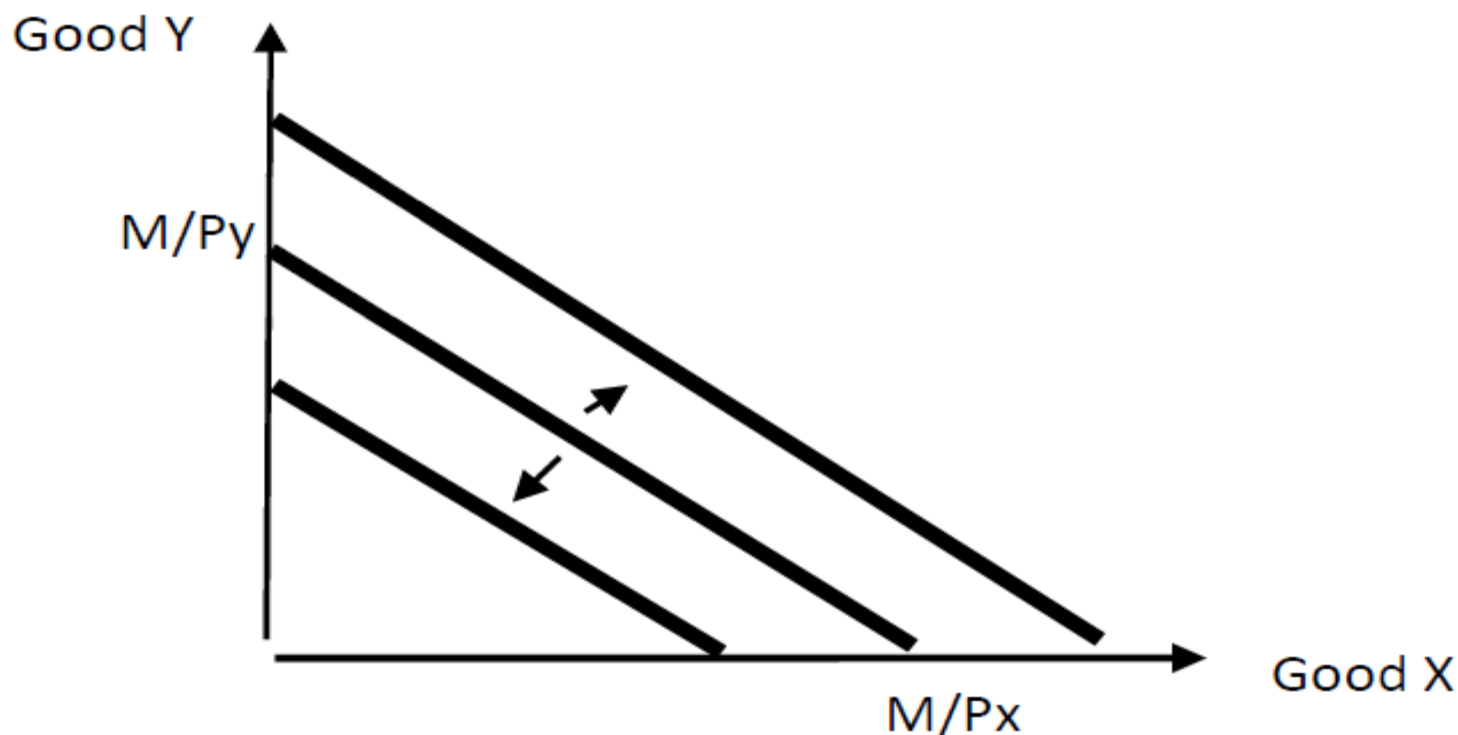
$$5Y = 100 - 3X$$

$$Y = \frac{100}{5} - \frac{3}{5}X$$

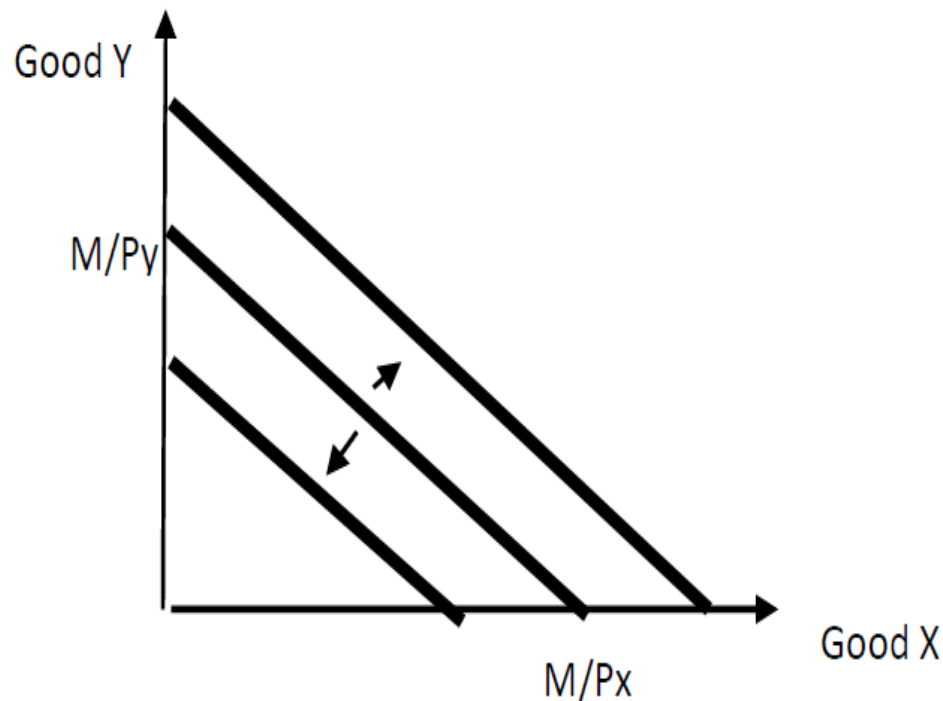
$$Y = 20 - \frac{3}{5}X$$



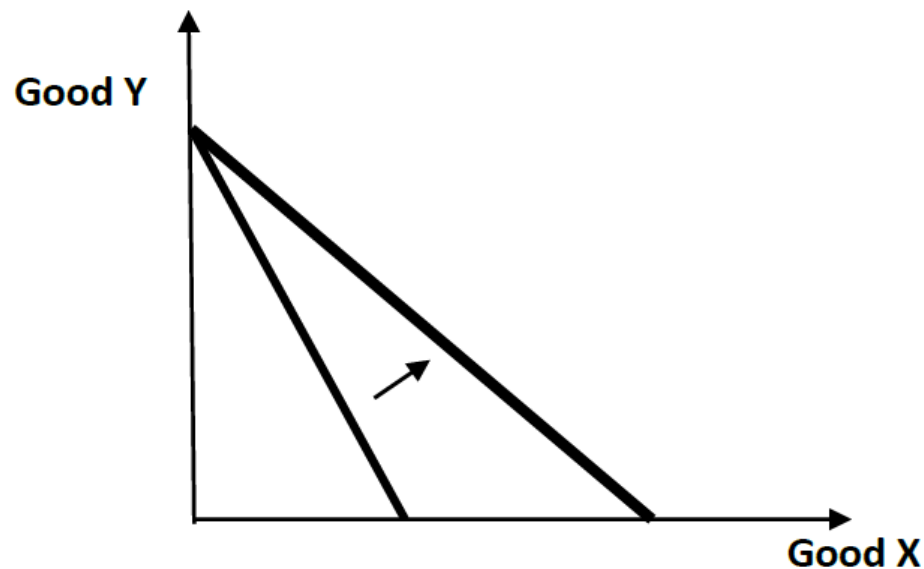
Change in income: If the income of the consumer changes (keeping the prices of the commodities unchanged), the budget line also shifts (changes). Increase in income causes an upward/outward shift in the budget line that allows the consumer to buy more goods and services and decreases in income causes a downward/inward shift in the budget line that leads the consumer to buy less quantity of the two goods. It is important to note that the slope of the budget line (the ratio of the two prices) does not change when income rises or falls.



Change in prices: An equal increase in the prices of the two goods shifts the budget line inward. Since the two goods become expensive, the consumer can purchase the lesser amount of the two goods. An equal decrease in the prices of the two goods, on the other hand, shifts the budget line outward. Since the two goods become cheaper, the consumer can purchase the more amounts of the two goods.

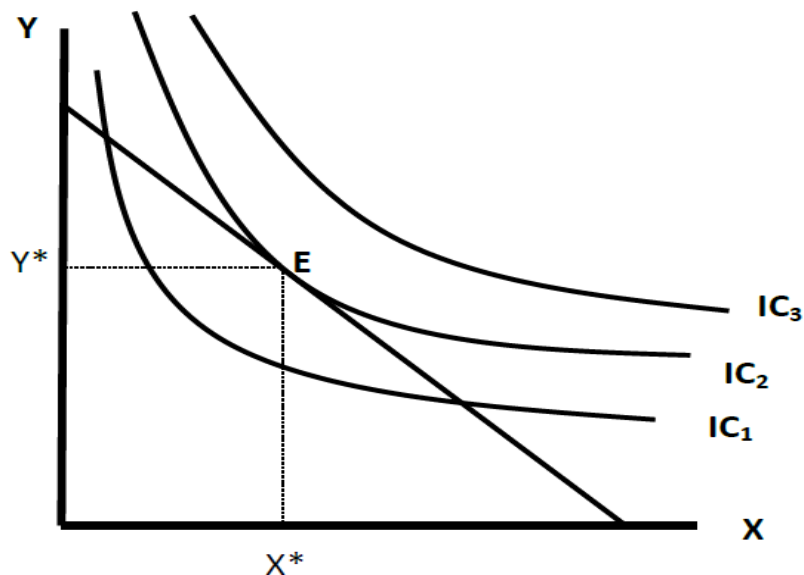


An increase or decrease in the price of one of the two goods, keeping the price of the other good and income constant, changes the slope of the budget line by affecting only the intercept of the commodity that records the change in the price. For instance, if the price of good X decreases while both the price of good Y and consumer's income remain unchanged, the horizontal intercept moves outward and makes the budget line flatter. The reverse is true if the price of good X increases. On the other hand, if the price of good Y decreases while both the price of good X and consumer's income remain unchanged, the vertical intercept moves upward and makes the budget line steeper. The reverse is true for an increase in the price of good Y.



Equilibrium of the consumer

The preferences of a consumer (what he/she wishes to purchase) are indicated by the indifference curve. The budget line specifies different combinations of two goods (say X and Y) the consumer can purchase with the limited income. Therefore, a rational consumer tries to attain the highest possible indifference curve, given the budget line. This occurs at the point where the indifference curve is tangent to the budget line so that the slope of the indifference curve (MRS_{XY}) is equal to the slope of the budget line (P_X / P_Y). In figure 3.10, the equilibrium of the consumer is at point 'E' where the budget line is tangent to the highest attainable indifference curve (IC_2).



Mathematically, consumer optimum (equilibrium) is attained at the point where:

Slope of indifference curve = Slope of the budget line

$$MRS_{XY} = \frac{P_X}{P_Y}$$
$$\Rightarrow \frac{MU_X}{MU_Y} = \frac{P_X}{P_Y}$$

Example: A consumer consuming two commodities X and Y has the utility function $U(X,Y) = XY + 2X$. The prices of the two commodities are 4 birr and 2 birr respectively. The consumer has a total income of 60 birr to be spent on the two goods.

- Find the utility maximizing quantities of good X and Y.
- Find the $MRS_{X,Y}$ at equilibrium.

Solution

a) The budget constraint of the consumer is given by:

$$P_X \cdot X + P_Y \cdot Y = M$$

$$4X + 2Y = 60 \dots\dots\dots (i)$$

Moreover, at equilibrium

$$\frac{MU_X}{MU_Y} = \frac{P_X}{P_Y}$$

$$\frac{Y + 2}{X} = \frac{4}{2}$$

$$\frac{Y + 2}{X} = 2$$

$$Y = 2X - 2 \dots\dots\dots (ii)$$

Substituting equation (ii) into (i), we obtain $Y = 14$ and $X = 8$.

$$b) \quad MRS_{X,Y} = \frac{MU_X}{MU_Y} = \frac{Y + 2}{X} = \frac{14 + 2}{8} = 2$$

(At the equilibrium, MRS can also be calculated as the ratio of the prices of the two goods)